Fundamental Symmetries and Weak Interaction through Parity Violation (Particularly with Polarized Electron Scattering)

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Modern Physics



Quantum Mechanics from Classical Mechanics

Matrix formulation of Hamiltonian in classical mechanics

Canonical invariants – Poisson brackets are invariant under canonical transformations

$$[u, v]_{q, p} = \frac{\partial u}{\partial q_1} \frac{\partial v}{\partial p_1} - \frac{\partial u}{\partial p_1} \frac{\partial v}{\partial q_1}.$$

Poisson bracket is replaced by an appropriate commutator for quantum mechanics

Much of the formal structure of quantum mechanics is a close copy of the Poisson bracket formulation of classical mechanics

Position and momentum are conjugate variables (Heisenberg uncertainty principle)

$$p \to \hat{p} = -i\hbar \frac{\partial}{\partial x}$$

If I have seen further it is by standing on the sholders [*sic*] of Giants Isaac Newton, 1676

Two components of L cannot simultaneously be canonical momenta

 \rightarrow L_i and L_i can't have simultaneous eigenvalues but L₂ can be quantized with any one of the L_i

EM as a (Classical) Gauge Theory

 $\mathbf{E} = abla \phi$

$$abla \cdot \mathbf{E} = 4\pi
ho$$
 $\nabla \times \mathbf{E} = -rac{1}{c}rac{\partial \mathbf{B}}{\partial t}$
 $abla \cdot \mathbf{B} = 0$
 $abla \times \mathbf{B} = rac{1}{c}\left(4\pi\mathbf{J} + rac{\partial \mathbf{E}}{\partial t}\right)$

$$\mathbf{E} = -
abla \phi - rac{\partial \mathbf{A}}{\partial t}$$
 $\mathbf{B} =
abla imes \mathbf{A}$

Scalar function
$$\psi(\vec{r},t)$$
 $\mathbf{A} \to \mathbf{A} + \nabla \psi$ Existence of arbitrary
numbers of $\psi(\vec{r},t)$ is the
U(1) "gauge freedom" $\varphi \to \varphi - \frac{\partial \psi}{\partial t}$

(Coulomb gauge $abla \cdot \mathbf{A}(\mathbf{r},t) = 0$) $\varphi(\mathbf{r},t) = rac{1}{4\piarepsilon_0} \int rac{
ho(\mathbf{r}',t)}{R} \,\mathrm{d}^3\mathbf{r}'$ $\mathbf{A}(\mathbf{r},t) =
abla imes \int rac{\mathbf{B}(\mathbf{r}',t)}{4\pi R} \,\mathrm{d}^3\mathbf{r}'$

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Local vs. Global

$$E_i = cF_{0i},$$

where c is the speed of light, and

$$B_i=-rac{1}{2}\epsilon_{ijk}F^{jk},$$

where ϵ_{ijk} is the Levi-Civita tensor.

$$F^{\mu
u} = \partial^\mu A^
u - \partial^
u A^\mu = egin{bmatrix} 0 & -E_x/c & -E_y/c & -E_z/c \ E_x/c & 0 & -B_z & B_y \ E_y/c & B_z & 0 & -B_x \ E_z/c & -B_y & B_x & 0 \end{bmatrix}$$

$${\cal L}=-rac{1}{4\mu_0}F_{\mu
u}F^{\mu
u}-J^\mu A_\mu$$

$$\psi(x) \rightarrow \psi(x) e^{i\alpha(x)},$$

 $A_{\mu}(x) \rightarrow A_{\mu}(x) - \frac{1}{q} \partial_{\mu}\alpha(x).$

Introduce covariant

derivative:

$$D_{\mu} = \partial_{\mu} + \mathrm{i}qA_{\mu}(x)$$

Restore local symmetry; $F^{\mu\nu}$ and Lagrangian are unchanged

Gauge fields – introduced to restore local symmetry – dictate the form of the couplings

Quantized EM \rightarrow QED

$$\mathcal{L} = ar{\psi} \left(i \hbar c \, \gamma^lpha \, D_lpha - m c^2
ight) \psi - rac{1}{4 \mu_0} F_{lpha eta} F^{lpha eta},$$

Creation and annihilation The fields of particles

The four-vectors are Lorentz covariant solutions to the Dirac equation (relativistic generalization of the Schrodinger equation)

The conserved vector current is:

$$j^{\mu} = -e\,\bar{\psi}\gamma^{\mu}\psi$$

$$\begin{split} \gamma^{0} &= \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}, \qquad \gamma^{1} = \begin{pmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{pmatrix} \\ \gamma^{2} &= \begin{pmatrix} 0 & 0 & 0 & -i \\ 0 & 0 & i & 0 \\ 0 & i & 0 & 0 \\ -i & 0 & 0 & 0 \end{pmatrix}, \qquad \gamma^{3} = \begin{pmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \\ -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix} \\ \gamma^{5} &:= i \gamma^{0} \gamma^{1} \gamma^{2} \gamma^{3} = \begin{pmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix} \end{split}$$

Discrete symmetries

Charge

 \hat{Q} is an operator that can measure the "charge", like the position and momentum operators \hat{x} and \hat{p}

$$|p\rangle = |\bar{p}\rangle$$

$$\mathsf{C}^{-1}\hat{Q}\mathsf{C} = -\hat{Q}$$



Credit: Quantum Field Theory for the Gifted Amateur

Not just EM charge, but also lepton number, hypercharge, etc.

Parity

$$\hat{x}\mathsf{P} = -\mathsf{P}\hat{x}.$$

$$\mathsf{P}^{-1}\hat{p}\mathsf{P} = -\hat{p}.$$

 $\mathsf{P}^{-1}\hat{x}\mathsf{P} = -\hat{x}.$

Time Reversal

 $\mathsf{T}^{-1}\hat{x}\mathsf{T}=\hat{x}$

perators \hat{x} and \hat{p}

The symmetries discussed so far were continuous: SU(3), SU(2) or U(1)

Discrete symmetries are represented by finite groups

quantum mechanical operator that reverses the spatial sign ($P: x \rightarrow x$)







We describe physical processes as interacting currents by constructing the most general form which is consistent with Lorentz invariance

Terms of the form $\overline{\psi} (4 \times 4) \psi$ where $\gamma^5 \equiv i \gamma^0 \gamma^1 \gamma^2 \gamma^3$

Scalar $\overline{\psi}\psi$ $\overline{\psi}\gamma^5\psi$ Pseudoscalar $\overline{\psi}\gamma^{\mu}\psi$ Vector $\overline{\psi}\gamma^{\mu}\gamma^{5}\psi$ Axial Vector $\overline{\psi}\sigma^{{}^{\mu
u}}\psi$ Tensor

Note: $P(V^*V) = +1$ $P(A^*A) = +1$ $P(A^*V) = -1$

NNPSS

EM and Weak Interactions : Historical View

EM: $e + p \rightarrow e + p$ elastic scattering



Weak: $n \rightarrow e^{-} + p + \bar{v}_e$ neutron beta decay

Fermi (1932) : contact interaction, form inspired by EM

$$M = J_{\mu}^{weak,N} G_{F} J^{\mu,weak,e} = \left(\overline{\psi}_{p} \gamma_{\mu} \psi_{n}\right) G_{F} \left(\overline{\psi}_{e} \gamma^{\mu} \psi_{v_{e}}\right)$$
$$V x V$$

Parity Violation (1956, Lee, Yang; 1957, Wu)

М

required modification to form of current - need axial vector as well as vector to get a parity-violating interaction

$$M = J_{\mu}^{weak,N} G_F J^{\mu,weak,e} = \left(\overline{\psi}_p \gamma_{\mu} \qquad \psi_n\right) G_F \left(\overline{\psi}_e \gamma^{\mu} \qquad \psi_{\nu_e}\right)$$

$$(V - A) \qquad x \qquad (V - A)$$

Note: weak interaction process here is charged current (CC)

Experiment

Can only measure something if it is "observable"



Transition rates or scattering cross sections

"Fermi's Golden Rule"

$$Fd\sigma = |M^2| dQ$$
$$\sigma \propto |M^2|$$

The incident flux times the differential cross section is proportional to the product of the square of the matrix element and the Lorentz invariant phase space

All the physics is in the matrix element

The Dirac Equation

Dirac equation for free electron: $(i\gamma^{\mu}\partial_{\mu} - m)\psi = 0$

where:

$$\gamma^{\mu} = \left(\gamma^{0}, \vec{\gamma}\right) \qquad \gamma^{0} = \left(\begin{matrix} \vec{1} & 0 \\ 0 & -\vec{1} \end{matrix}\right) \qquad \vec{\gamma} = \left(\begin{matrix} 0 & \vec{\sigma} \\ -\vec{\sigma} & 0 \end{matrix}\right)$$

with:
$$\mu = 0$$
 time, $\mu = 1,2,3$ space

leads to electron four-vector current density:

$$j^{\mu}=-e\;\overline{\psi}\gamma^{\mu}\psi$$
 where the adjoint is: $\overline{\psi}\equiv\psi^{+}\gamma^{0}$

satisfies the continuity equation:

$$\partial_{\mu}j^{\mu}=0$$

the matrix element



the matrix element



Atomic Parity Violation

Z-boson exchange between atomic electrons and the quarks in the nucleus H_{PNC} mixes electronic s & p states • V_e $< n's' \mid H_{PNC} \mid np > \propto Z^3$ Drive $s \rightarrow s E1$ transition! Z⁰ 70 70 $Q_W = 2(\kappa_{1p}Z + \kappa_{1n}N)$ W[±],Z⁰ Ν Ν $\kappa_{1p} = \frac{1}{2}(1 - 4\sin^2\theta_W), \kappa_{1n} = -\frac{1}{2}$ PV hadronic interactions hyperfine correction to NSD Z-exchange \Rightarrow PV anapole moment the weak neutral current of the nucleus

nucl. spin *independent* interaction coherent over all nucleons

$$H_{\rm PNC}^{nsi} = \frac{G}{\sqrt{2}} \frac{Q_W}{2} \gamma_5 \,\delta(\mathbf{r}).$$

Cs: 6s \rightarrow 7s osc. strength f \approx 10⁻²² use interference:

> $f \propto |A_{PC} + A_{PNC}|^{2}$ $\approx A_{PC}^{2} + A_{PC} A_{PNC} \cos \varphi$

nucl. spin *dependent*, interaction only with valence nucleons

Credit: Gerald Gwinner

Hadronic Weak Interaction at Low Energies

$$\mathcal{H}_{W}^{\Delta S=0} = \frac{G_{F}}{2\sqrt{2}} [\cos^{2}\theta_{W}J_{\mu}^{W,0\dagger}J^{W,0\mu} + \sin^{2}\theta_{W}J_{\mu}^{W,1\dagger}J^{W,1\mu} + J_{\mu}^{Z\dagger}J^{Z\mu}]$$

- Initial motivation: Neutral weak currents can be accessed via $\Delta S = 0$, $\Delta I = 1$
- Systems that can access HWI:
 - few body nucleon-nucleon (NN) interactions
 - large level spacings, small PV admixtures
 - need lots of statistics
 - n-p, p-p, n-d, n-³He, n-⁴He, p-⁴He, γ -d, etc.
 - nuclear systems
 - small level spacings, large PV admixtures, not as theoretically clean

NNPSS

- not a lot of statistics needed
- ¹⁸F, ¹⁹F, many more heavier compound neuclei

Strategy: NPDGamma and other few nucleon systems work really hard to

measure 10^{-8} asymmetries. Theory is reliable and interpretable.

Gluon exchange/Meson exchange

Hadronic Weak Interaction: Theories

An Overview:

• DDH meson exchange model: PV potential π , ρ , and ω with strong and weak vertex. 7 Weak couplings h_{π}^1 , $h_{\rho}^{0,1,2}$, $h_{\rho}^{1\prime}$, and $h_{\omega}^{0,1}$ B. Desplanques, J. F. Donoghue, and B. R. Holstein, Annals of Physics, 124 (1980) W. C. Haxton and B. R. Holstein, Progress in Particle and Nuclear Physics (2013) • EFT(π , π), χ EFT: 5 LEC constants, model independent S. L. Zhu et al., Nucl. Phys. A748 (2005) 435 $g_{\pi NN} g_{\omega} g_{\rho}$ L. Girlanda, Phys. Rev. C77 (2008) 067001 D. R. Phillips, M. R. Schindler, and R. P. Springer, Nucl. Phys. A822 (2009) 1 • $1/N_c$ expansions: $N_c \rightarrow$ large gives hierarchy of couplings D. Phillips, D. Samart, and C. Schat, PRL 114 (2015) 062301 relative scale $\sim m_\pi/m_W \sim 10^{-7}$ M. R. Schindler, R. P. Springer, and J. Vanasse, PRC 93 (2016) 025502 Gardner, Haxton, Holstein, ARNPS 67, 69 (2017)

NNPSS

Hadronic Weak interaction: NPDGamma

NPDGamma $(\vec{\sigma} \cdot \vec{k})$ at the SNS at ORNL, goal: $h_{\pi}^{1} \sim 1 \times 10^{-7}$

- Flipping the neutron polarization is equivalent to a parity transformation
- NPDG measures the asymmetry between the neutron polarization and the emitted photon's momentum
- Large statistics! Must collect 10¹⁶ photons to see 10⁻⁸ asymmetry!

$$\frac{d\sigma}{d\Omega} \propto \frac{1}{4\pi} \left(1 - 2\sqrt{2} \frac{\langle \mathbf{E} \mathbf{1} \rangle}{\langle \mathbf{M} \mathbf{1} \rangle} \cos\theta \right), \quad A_{\gamma} \equiv -2\sqrt{2} \frac{\langle \mathbf{E} \mathbf{1} \rangle}{\langle \mathbf{M} \mathbf{1} \rangle}, \quad A_{\gamma} = \frac{\frac{d\sigma}{d\Omega} + -\frac{d\sigma}{d\Omega}}{\frac{d\sigma}{d\Omega} + +\frac{d\sigma}{d\Omega} - \frac{d\sigma}{d\Omega}}$$

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da

Credit: Jason Fry

Hand-waving derivation of the parity-violating asymmetry in electron-proton scattering

$$J_{\mu}^{EM,e} = Q_e \overline{\psi}_e \gamma_{\mu} \psi_e = Q_e V_{\mu}^{EM,e}$$

 $J_{\mu}^{\,{\scriptscriptstyle E\!M\,},{\scriptscriptstyle N}}=V_{\mu}^{\,{\scriptscriptstyle E\!M\,},{\scriptscriptstyle N}}$

$$M_{EM} \sim \frac{1}{Q^2} J_{\mu}^{EM,e} J_{\mu}^{EM,p} \sim \frac{1}{Q^2} Q_e V_{\mu}^{EM,e} V_{\mu}^{EM,N}$$

$$J_{\mu}^{NC,e} = \left(-1 + 4\sin^2\theta_W\right)\overline{\psi}_e\gamma_{\mu}\psi_e + \overline{\psi}_e\gamma_5\gamma_{\mu}\psi_e$$

$$J_{\mu}^{NC,N} = V_{\mu}^{NC,N} + A_{\mu}^{NC,N}$$

$$M_{NC} \sim \frac{G}{2\sqrt{2}} J_{\mu}^{NC,e} J_{\mu}^{NC,p} \sim \frac{G}{2\sqrt{2}} \Big[g_{V}^{e} V_{\mu}^{NC,e} V_{\mu}^{NC,N} + g_{A}^{e} A_{\mu}^{NC,e} V_{\mu}^{NC,N} + g_{V}^{e} V_{\mu}^{NC,e} A_{\mu}^{NC,e} A_{\mu}^{NC$$

Asymmetry

$$\sigma_{\pm} \propto [M_{EM} \pm M_{NC}]^2 = |M_{EM}|^2 \pm 2Re(M_{EM}^* M_{NC}) + |M_{NC}|^2$$

$$A_{PV} = \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-}$$

$$\Rightarrow \frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \frac{\left(Q_e V_{\mu}^{EM,e} V_{\mu}^{EM,N} g_A^e A_{\mu}^{NC,e} V_{\mu}^{NC,N} + Q_e V_{\mu}^{EM,e} V_{\mu}^{EM,N} g_V^e V_{\mu}^{NC,e} A_{\mu}^{NC,N}\right)}{\left(Q_e V_{\mu}^{EM,e} V_{\mu}^{EM,N}\right)^2}$$

Elastic Scattering

 ${
m Q}^2$ is related to the wavelength of the virtual photon probe - $\;\lambda=h\,/\,q$

Cartoon Experiment

Blinding

Why would anyone want to "hide" the result from oneself?

The need for blind analysis (in fact, *double-blind* analysis in which the subject (the patient) and the researcher are both unaware of who is getting the medicine and who is getting the placebo) is well established in medicine – no clinical trial is taken seriously unless it is *double-blind*.

Double-blind technique first used in 1942

But, you say, we are **physicists** – rigorous, objective, unbiased...

Why should we want to blind?

Suggestions for further reading*:

Credit: D. Armstrong

- Joshua R. Klein, Aaron Roodman, Annu. Rev. Nucl. Part. Sci. 2005. 55:141
- P. F. Harrison, J. Phys. G: 28 2679 (2002)
- F.G. Dunnington, Phys. Rev. 43, 404, (1933).
- R. Feynman, "Surely You're Joking, Mr. Feynman!" New York: W.W. Norton (1985)

*much of this talk shamelessly borrowed from these sources

Examples

mean lifetime (ps)

0X 85

95

90

2.0

1.8

1.6 (ps)

mean

ħ

.2

1.0

1100

1050

1000

950

900

Neutron lifetime (s)

The speed of light vs. year

Just a coincidence that there are several measurements in a row that have close to the same central values?

Even with such large uncertainties?

ΞŦΞ

When to Blind

Armstrong's criterion:

Blinding is a good idea* for any analysis in which:

a) there is judgment involved - eg. setting cuts, choosing data sets, deciding on background subtraction techniques, which polarimeter to trust, linear regression vs. beam modulation, Q² ambiguities, GEANT 3 vs GEANT 4 radiative corrections, *etc.*

and

b) there is an "expected" answer, eg. from precise previous experiments or theoretical prediction – eg. Standard Model tests!

*translation: absolutely flipping essential

Credit: D. Armstrong

Unconscious (?) bias

An experimenter's natural tendency is to looks for bugs or additional systematic errors when a result does not agree with expectation, and to not look so hard if it does...as well, to only look for those systematic errors that will work in the "right direction" to "explain" the deviation....

Blinding prevents this from happening – all systematics are treated in an unbiased, objective manner

But, you say, what if I remove the blinding, and my result is "crazy" (say, 6 σ from Standard Model) – aren't there lots of checks I should do before I publish?

Answer: make a list of all those checks and studies and do them all *before* you unblind – if you haven't done them all, you don't deserve to publish a test of the Standard Model !!

Credit: D. Armstrong

Aside: blinding, of course, is no protection against deliberate fraud by experimenter...

Measuring A_{PV} with ES

- unpolarized target
- high current
- highly polarized beam

- polarimetry
- elastic electrons from target (resolution of the spectrometers)
- beam property monitoring
- active feedback to minimize helicity correlations
- rapid helicity reversal
- slow helicity reversal as a cross check

Statistical Uncertainty on A_{PV}

The statistical uncertainty in a counting experiment is given by

$$\sigma_N = \sqrt{N}$$
 $\frac{\delta N}{N} = \frac{\sqrt{N}}{N} = \frac{1}{\sqrt{N}}$

 $A_{meas} = \frac{N_1 - N_2}{N_1 + N_2}$

The expected width, σ_A , is calculated from

$$\sigma_A^2 = \sum \sigma_{N_i}^2 \left(\frac{\partial A}{\partial N_i}\right)^2$$

 $\sigma_{N_i} = \sqrt{N_i}$

Hint:

$$\frac{\partial A}{\partial N_1} = \frac{2N_2}{(N_1 + N_2)^2} \qquad \qquad \frac{\partial A}{\partial N_2} = \frac{-2N_1}{(N_1 + N_2)^2} \qquad \qquad N_1 \sim N_2 = \frac{N_1}{2}$$

$$\sigma_A^2 = N_1 \left(\frac{2N_2}{(N_1 + N_2)^2} \right)^2$$

Statistical Uncertainty

Jefferson Lab

Parity quality beam >85% using strained GaAs photocathodes ~100 μA max (multi-hall running)

After upgrade to 12 GeV beam energy, addition of a new Hall D

Polarized Electron Source

photoemission of electrons from GaAs

 \rightarrow "Bulk" GaAs typical P_e ~ 37% theoretical maximum - 50%

 \rightarrow "Strained" GaAs = typical P_e ~ 80% theoretical maximum - 100%

"Figure of Merit" $\propto 1 P_e^2$

Helicity reversals

• Feedback on Intensity Asymmetry

Precision Polarimetry

Require measurement of the beam polarization to sub-

Strategy: use 2 independent polarimeters

dP/P = 1%

- Use existing Hall C Møller polarimeter to measure absolute beam polarization to <1% at low beam currents
- Known analyzing power provided by polarized Iron foil in high magnetic field

- Use Compton polarimeter to provide continuous, non-destructive measurement of beam polarization
- Known analyzing power provided by circularly-polarized laser beam

Compton Polarimeter

Fabry-Perot Optical Cavity $\alpha_{c} = 1.346^{\circ}$ $P_{L} = 10kW$ $\lambda = 532nm$ $(1 + \cos(\alpha_{c})) - L - P_{L} \rightarrow 1$

$$\mathcal{L} \simeq \frac{(1.+\cos(\alpha_c))}{\sqrt{2\pi}} \frac{I_e}{e} \frac{P_L \lambda}{h c^2} \frac{1}{\sqrt{\sigma_e^2 + \sigma_\gamma^2}} \frac{1}{\sin(\alpha_c)}$$

Analyzing Power, 11 GeV and 1064 nm

$$\sigma_{\gamma}^2 = 80 \mu m$$

$$\sigma_e^2 = 80 \mu m$$

$$\sigma_{tot} = 49 \, fm^{-2}$$

False asymmetries from helicity correlated beam properties

50,000 nanometers!!!