

Precision Mass Measurements of Short-lived Nuclei at the HIRFL-CSR facility: N = 32 subshell closure in Scandium

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Outline

1

**Introduction:
Mass Measurements**

2

**Motivation:
Magic number $N=32$**

3

**IMS Experiment:
Setup, Analysis**

4

Results and Discussion

5

Future Improvements



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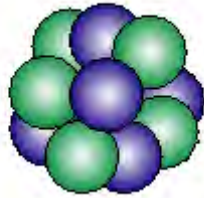
5

Future Improvements





Atomic Mass

Mass \rightarrow Binding Energy \rightarrow Interaction



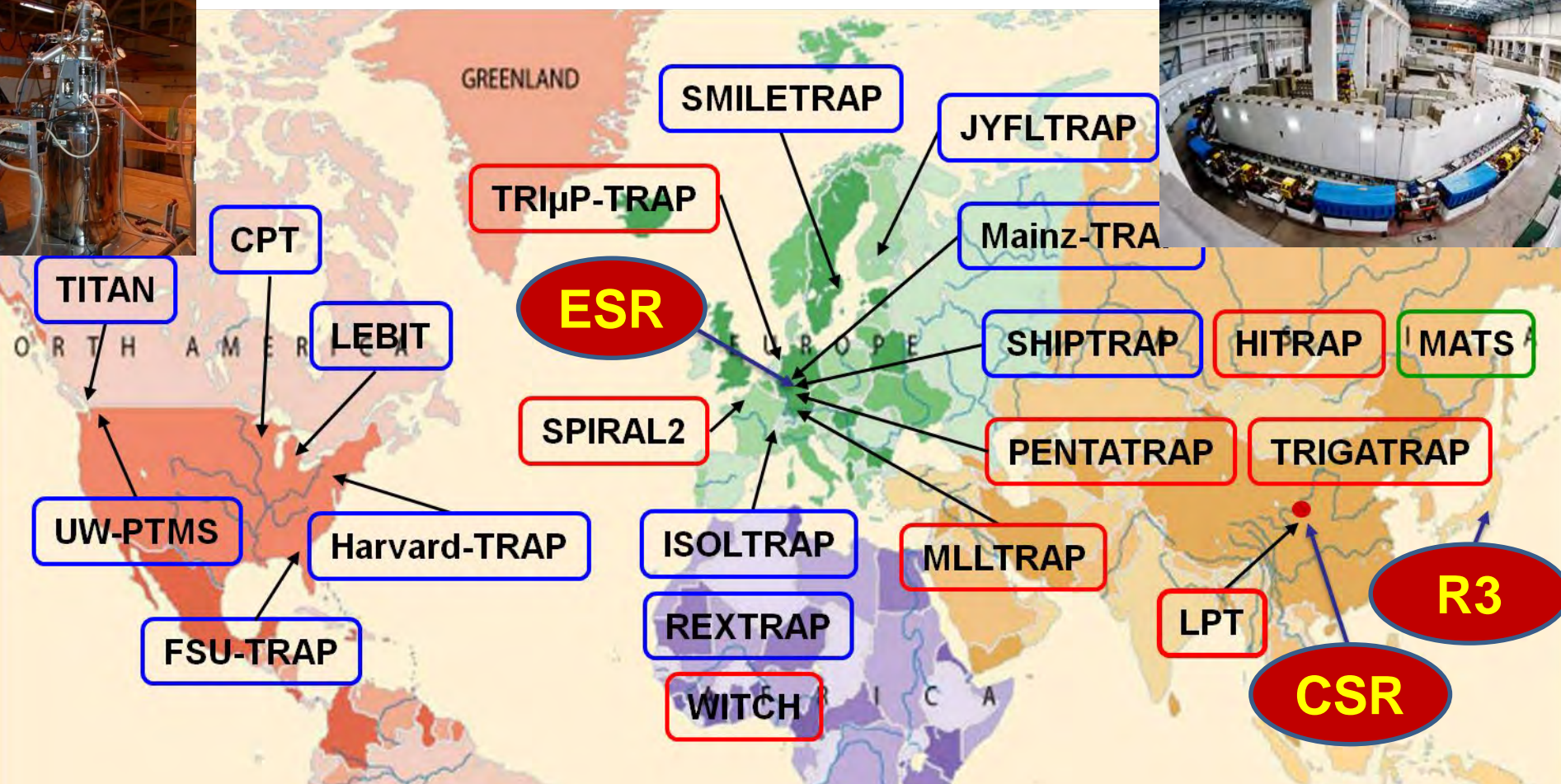
$$= N \times \text{green sphere} + Z \times \text{purple sphere} - \text{Binding Energy}$$


Nuclear Mass Measurement


Filed of application	Required uncertainty
Chemistry: identification of molecules	$10^{-5} - 10^{-6}$
Nuclear physics: shells, sub-shells, pairing	10^{-6} ~100 keV
Nuclear structure: deformation, halos	$10^{-7} - 10^{-8}$
Astrophysics: r-process, rp-process, waiting points	10^{-7} ~10 keV
Nuclear models and formulas: IMME	$10^{-7} - 10^{-8}$
Weak interaction studies: CVC hypothesis, CKM unitarity	10^{-8} ~1 keV
Atomic physics: binding energies, QED	$10^{-9} - 10^{-11}$
Metrology: fundamental constants, CPT	10^{-10}



Penning Traps & Storage Rings



Penning Trap:
Highest precision (10^{-5} - 10^{-11})
Lifetime: \sim s
Phase-Imaging Tech (\sim 100 ms)

Storage ring:
High precision (10^{-5} - 10^{-7})
Short-lived ($>100\mu$ s),
low production



Atomic Mass Evaluation (AME)



The NUBASE2016 evaluation of nuclear properties,
Chinese Physics C Vol. 41, No. 3 (2017) 030001

*The AME 2016 atomic mass evaluation (1):
evaluation of input data, adjustment procedures,*
Chinese Physics C Vol. 41, No. 3 (2017) 030002

*The AME 2016 atomic mass evaluation (2): tables,
graphs and references,*
Chinese Physics C Vol. 41, No. 3(2017) 030003



"ATOMIC MASS DATA CENTER"

<http://amdc.impcas.ac.cn/>

Andoid: Google Play Store request "Nucleus Amdc"

Win: http://amdc.impcas.ac.cn/web/nubdisp_en.html

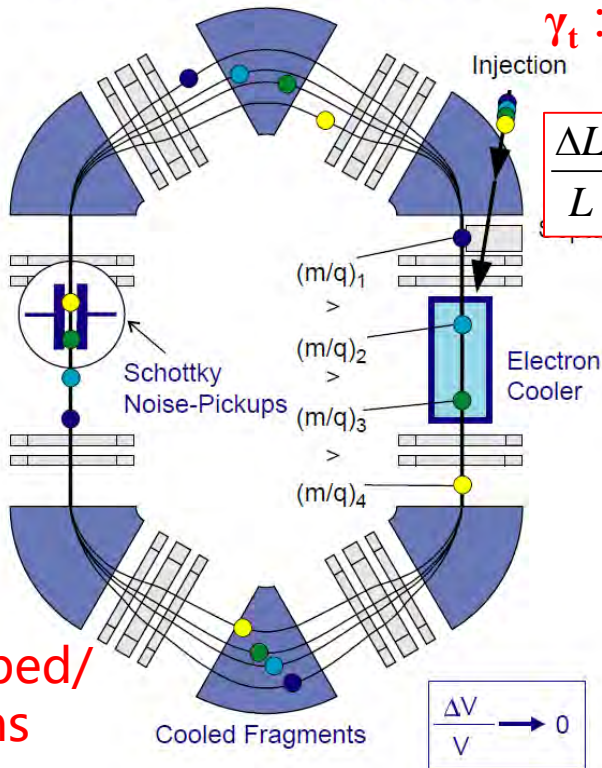


Storage-ring Mass Spectrometry

Frequency $\rightarrow \frac{\Delta f}{f} = -\frac{1}{\gamma_t^2} \frac{\Delta(m/q)}{(m/q)} + \left(1 - \frac{\gamma^2}{\gamma_t^2}\right) \frac{\Delta v}{v}$

γ : Lorentz factor
 v : Velocity

SCHOTTKY MASS SPECTROMETRY

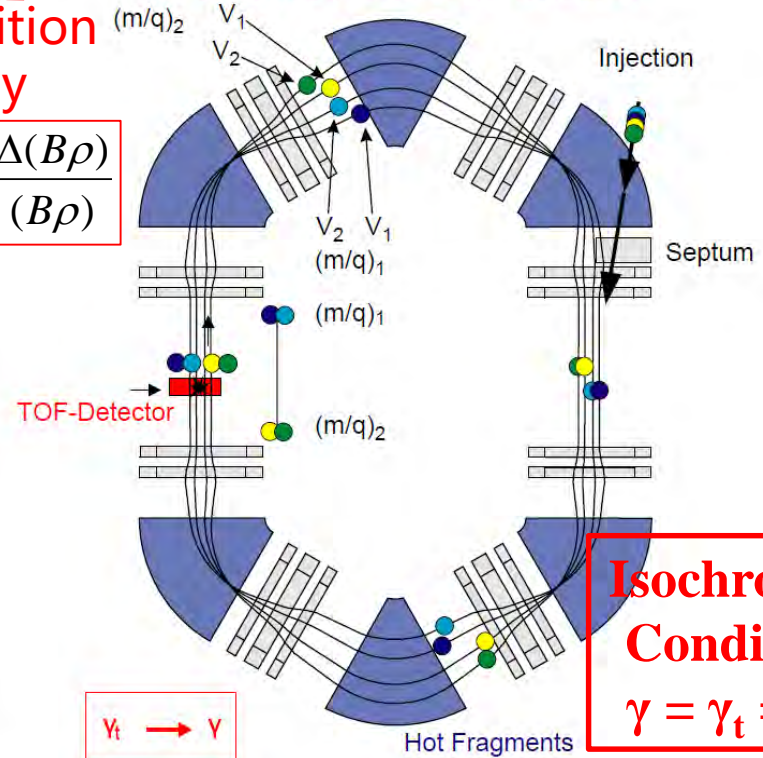


Fully stripped/
H⁺-like ions

γ_t : Transition Energy

$$\frac{\Delta L}{L} = -\frac{1}{\gamma_t^2} \frac{\Delta(B\rho)}{(B\rho)}$$

ISOCRONOUS MASS SPECTROMETRY



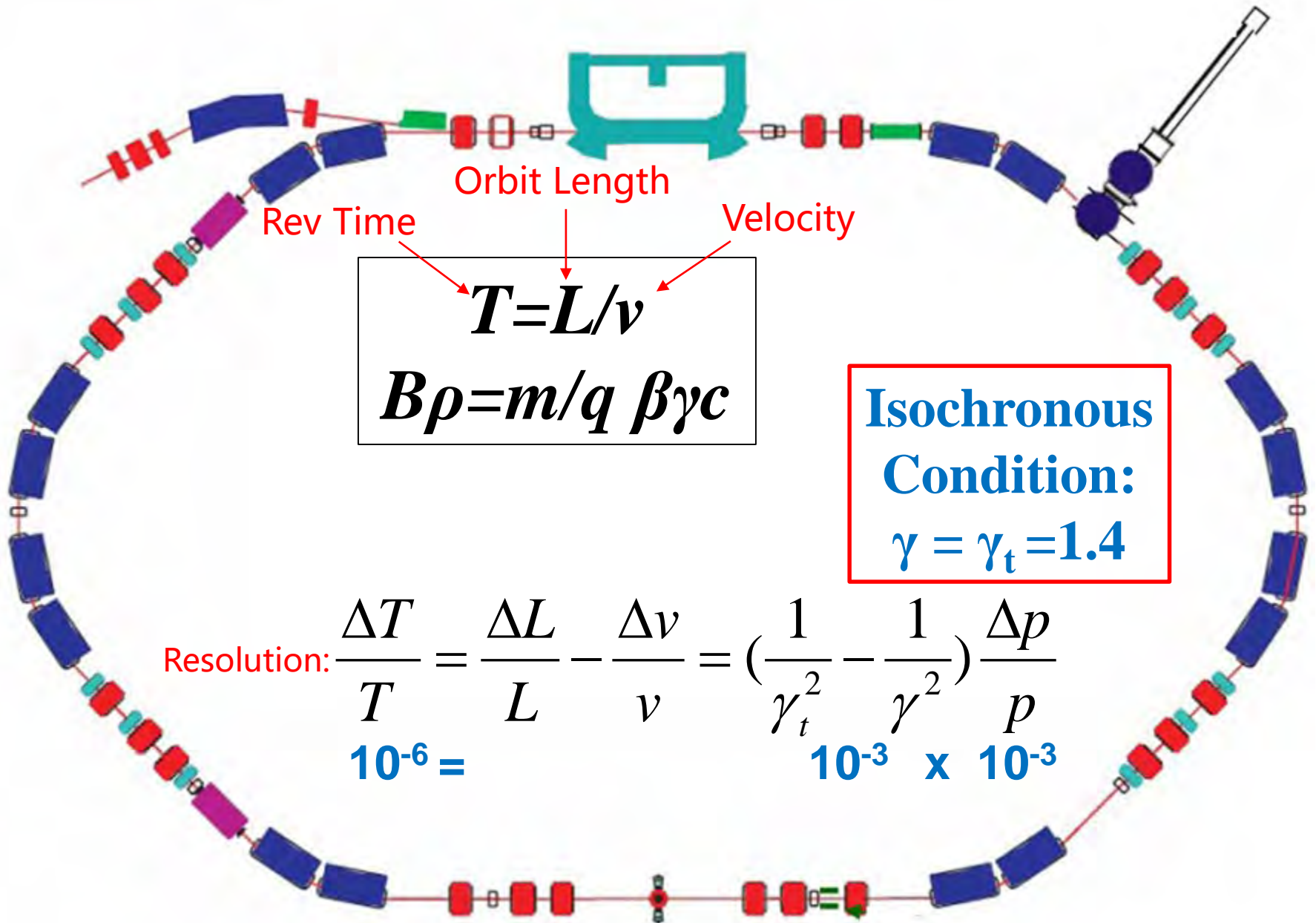
Isochronous Condition:
 $\gamma = \gamma_t = 1.4$

Schottky Mass Spectrometry (SMS):
 Relative High precision (10⁻⁷-10⁻⁸)
 Lifetime: ~ s

Isochronous Mass Spectrometry (IMS) :
 precision (10⁻⁵-10⁻⁷)
 Short-lived: >100us



Basic Principle of IMS





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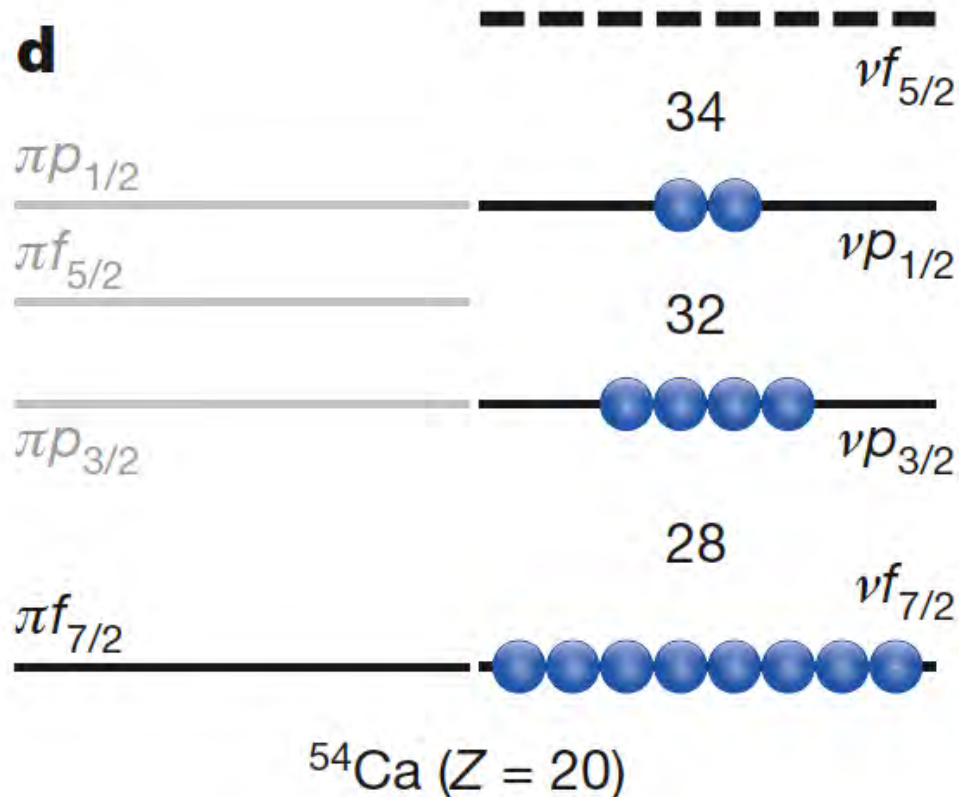


Shell Evolution in Neutron-rich Nuclei

Otsuka, et al, Evolution of Nuclear Shells due to the Tensor Force, PRL 95, 232502 (2005)

$$j_{>} = l + 1/2$$

$$j_{<} = l - 1/2$$



D. Steppenbeck¹, et al, NATURE 502, 207 (2013)



➤ **Enhanced excitation energies of first 2^+ states**

D. Steppenbeck et al., Phys. Rev. Lett. 114, 252501 (2015).

A. Huck, et. Al., Phys. Rev. C 31, 2226 (1985).

R. V. F. Janssens et al., Phys. Lett. B 546, 55 (2002).

J. I. Prisciandaro et al., Phys. Lett. B 510, 17 (2001).

➤ **Reduced gamma-ray transition probabilities**

D.-C. Dinca et al., Phys. Rev. C 71, 041302(R) (2005).

A. Büeger et al., Phys. Lett. B 622, 29 (2005).

➤ **S_{2n} and Empirical shell gap**

A. T. Gallant et al., Phys. Rev. Lett. 109, 032506 (2012).

F. Wienholtz et al., Nature (London) 498, 346 (2013).

M. Rosenbusch et al., Phys. Rev. Lett. 114, 202501 (2015).

E. Leistenschneider et al., Phys. Rev. Lett. 120, 062503 (2018).

M. P. Reiter et al., Phys. Rev. C 98, 024310 (2018).

C. Guenaut et al., J. Phys. G: Nucl. Part. Phys. 31, S1765 (2005).



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HIRFL-CSR Facility

Heavy Ion Research Facility in Lanzhou & Cooler Storage Ring Facility



SSC (K=450)
100 AMeV (H.I.), 110 MeV (p)

Pre-Accelerator



SFC (K=69)
10 AMeV (H.I.), 17~35 MeV (p)



Storage ring

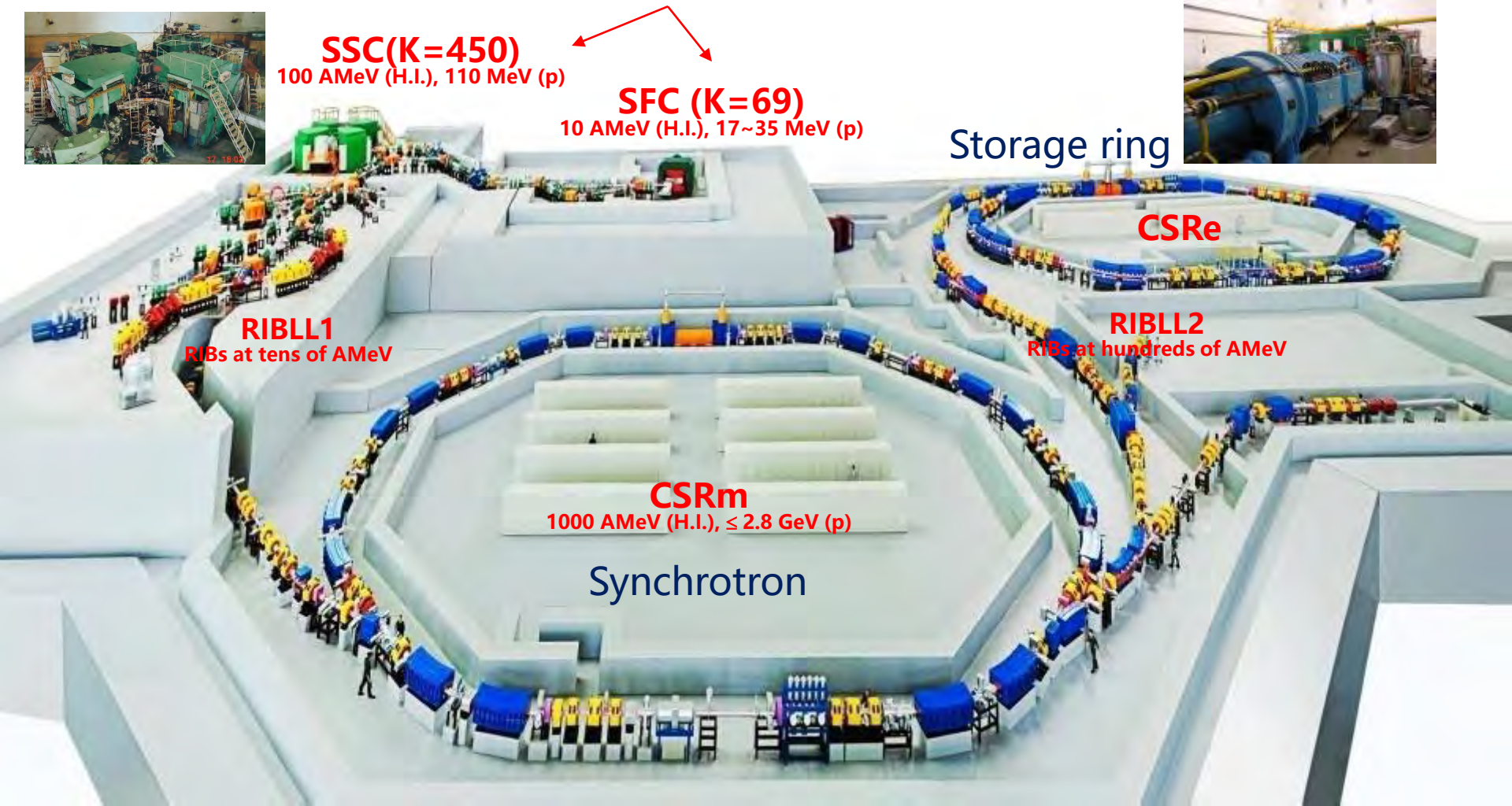
CSRe

RIBLL1
RIBs at tens of AMeV

RIBLL2
RIBs at hundreds of AMeV

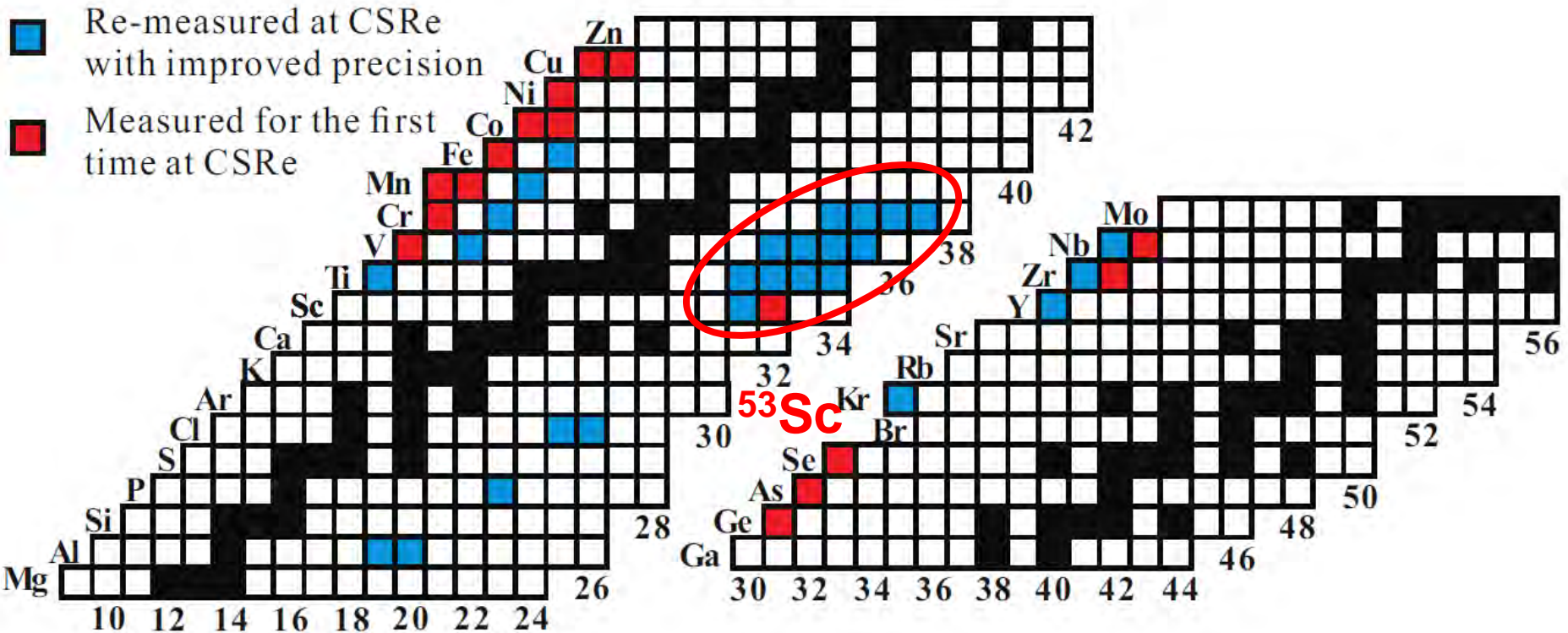
CSRm
1000 AMeV (H.I.), ≤ 2.8 GeV (p)

Synchrotron



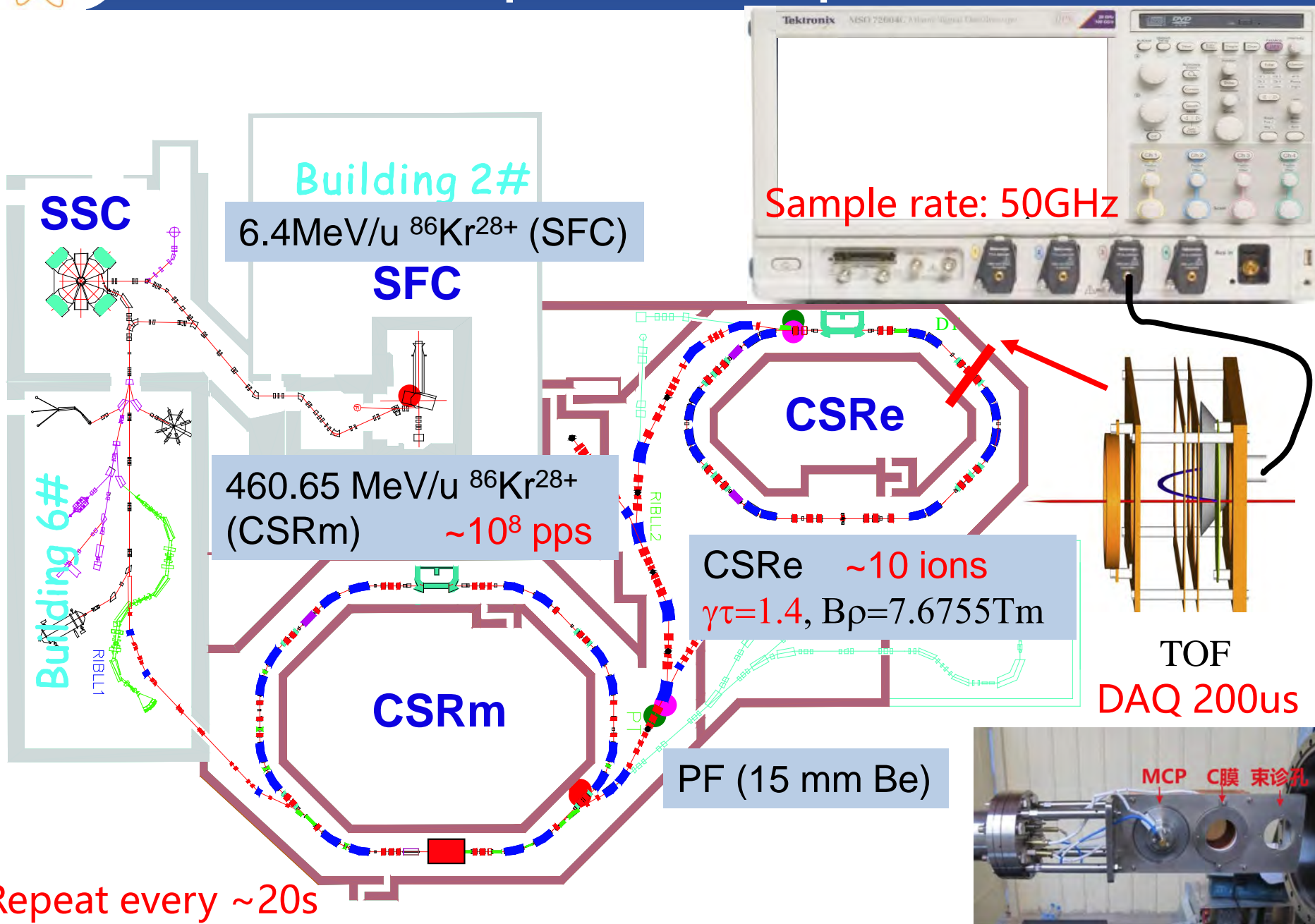


Experiment Objective



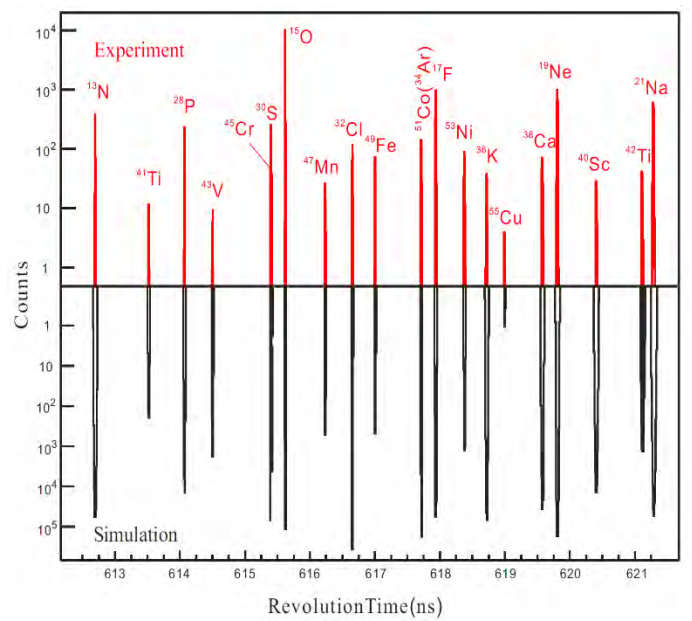
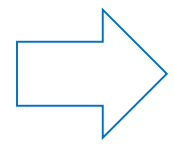
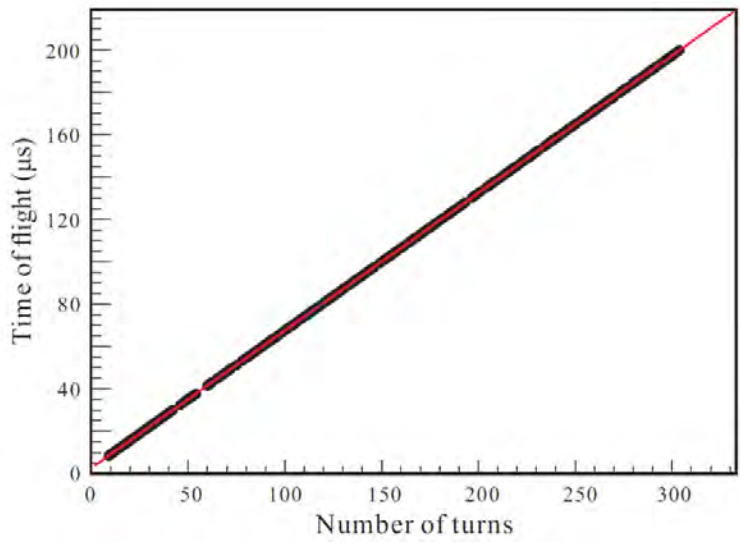
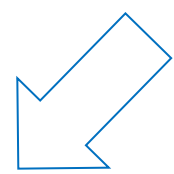
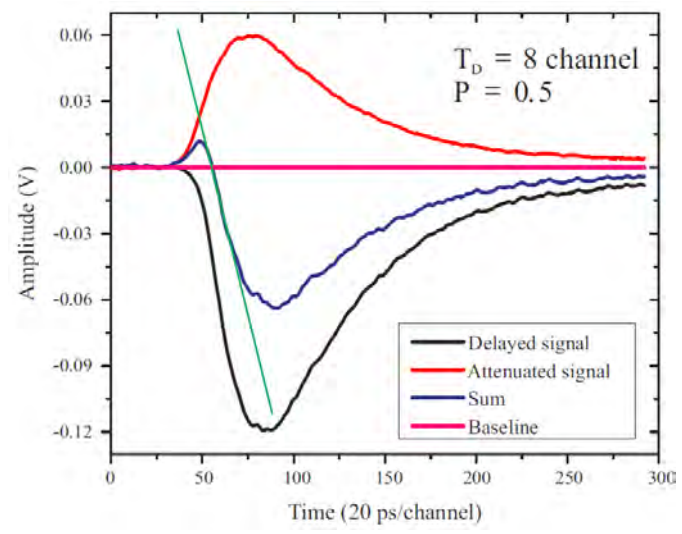
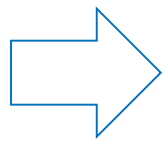
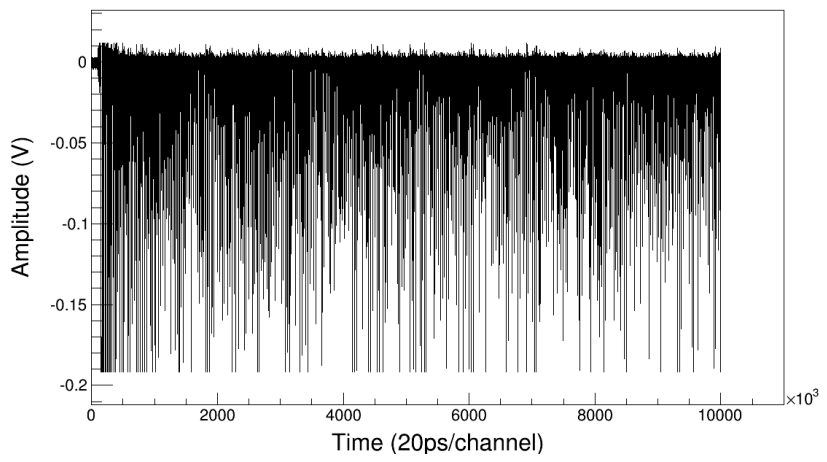


IMS experiment procedure



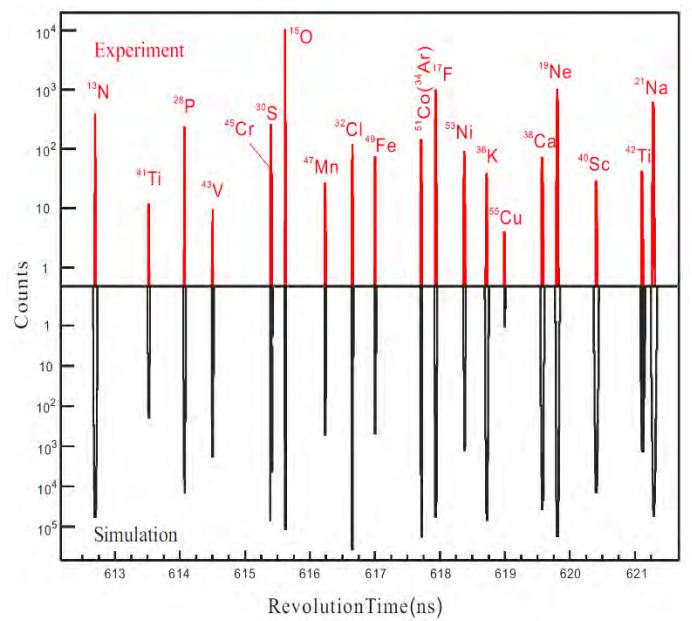
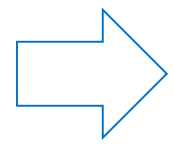
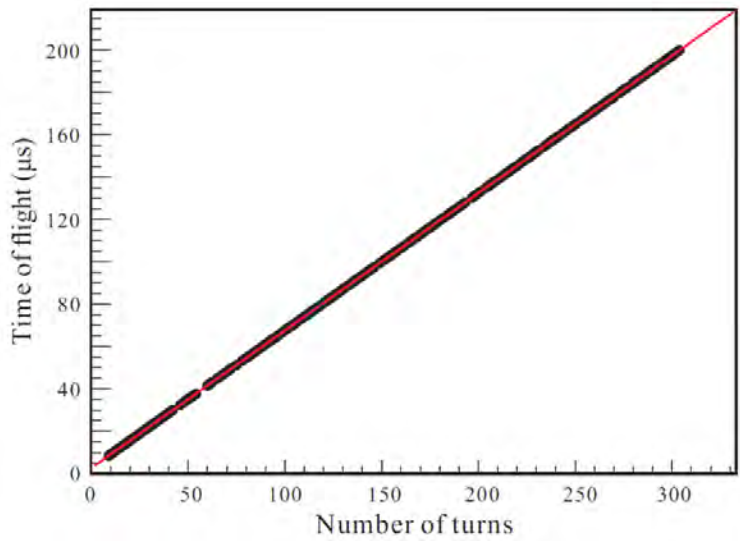
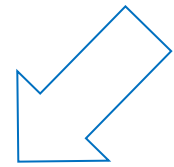
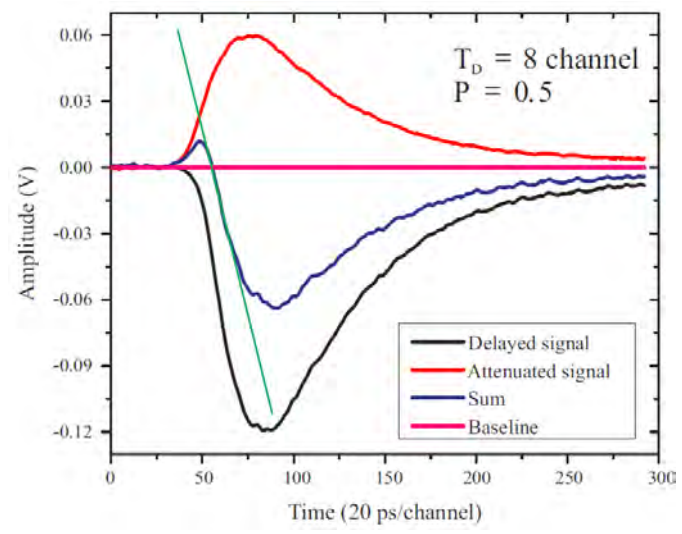
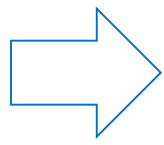
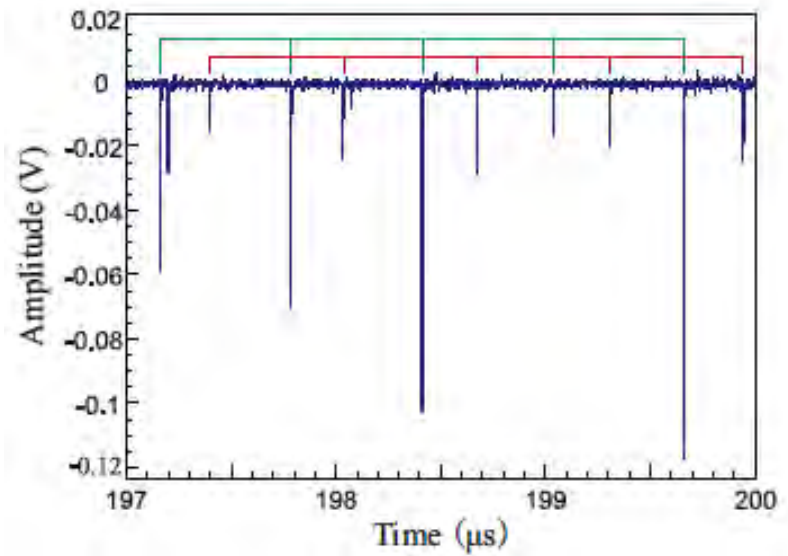


IMS Data Analysis



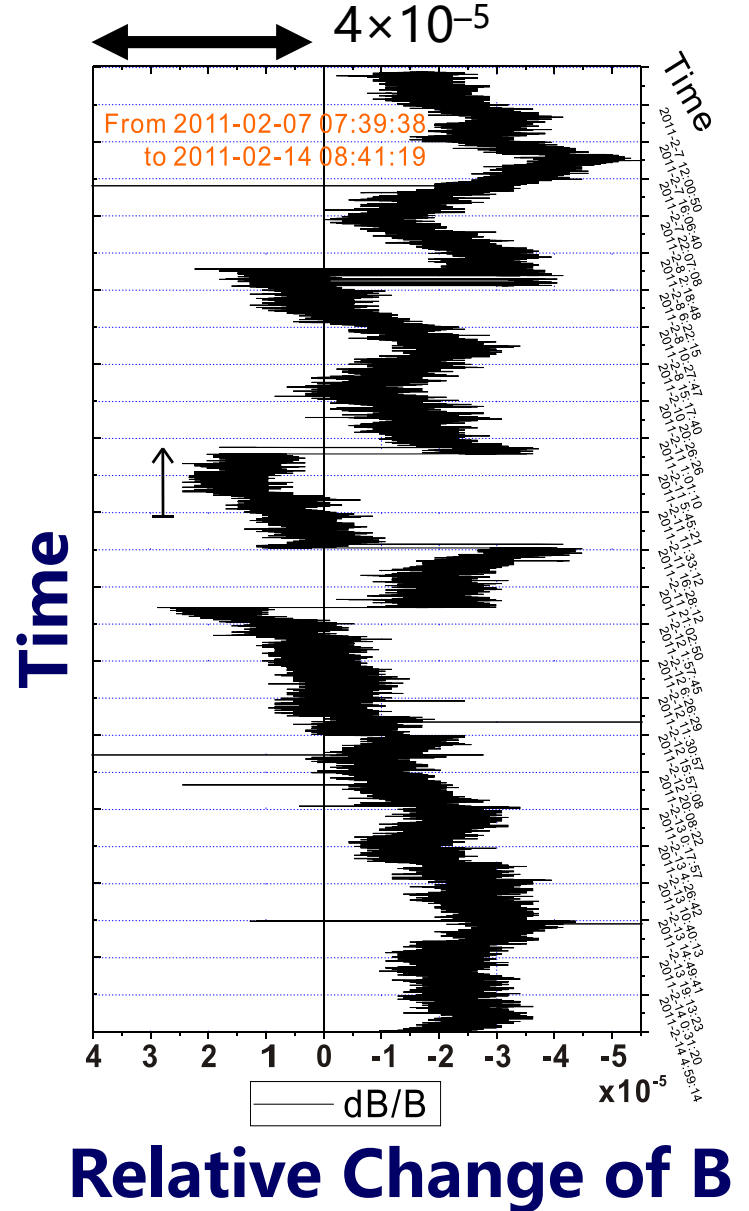
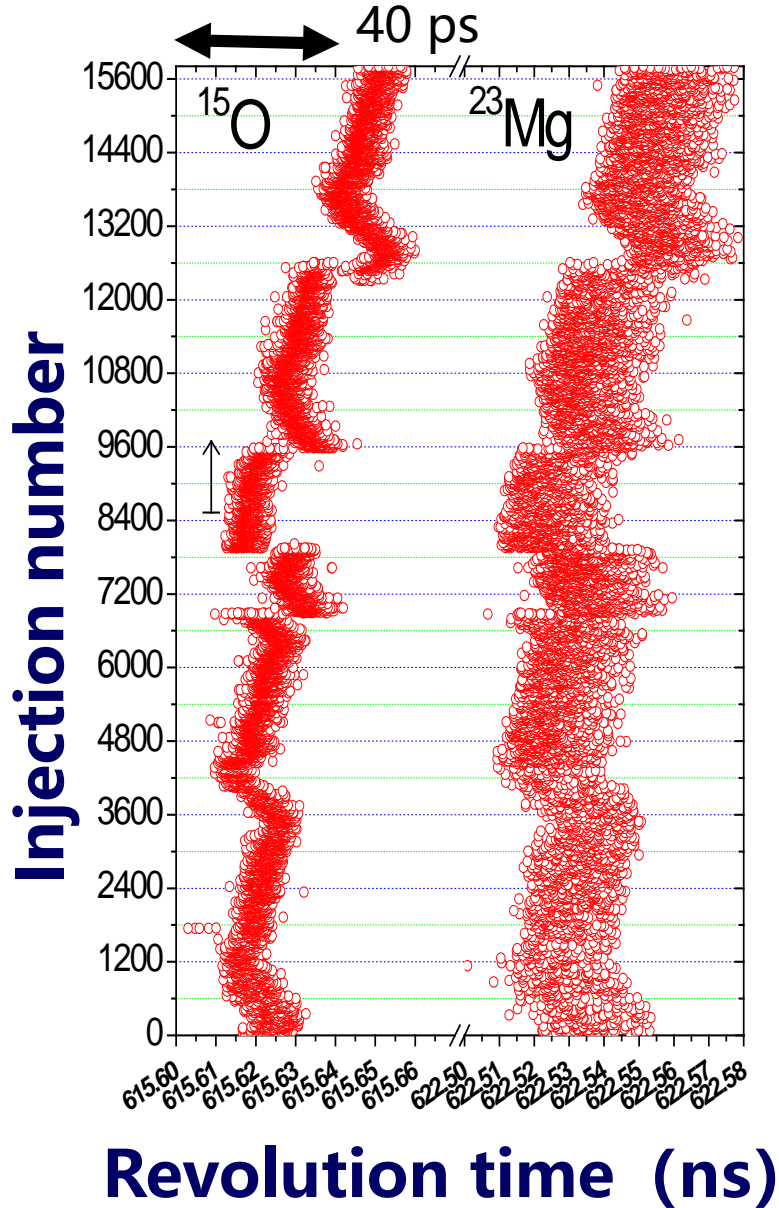


IMS Data Analysis





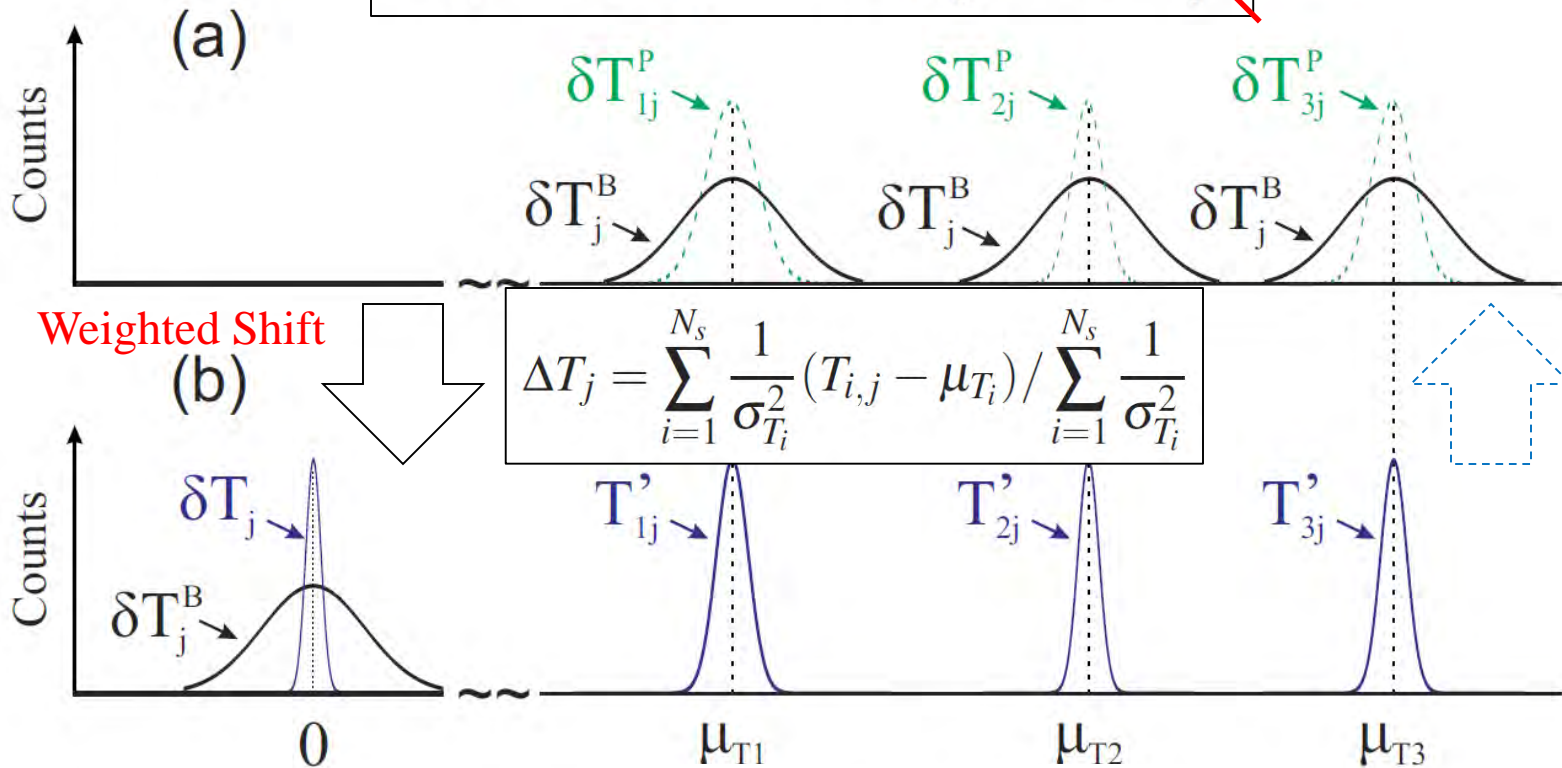
Unstable Magnetic field





Weighted Shift Correction

$$T_{i,j} = \mu_{T_i} + \delta T_{i,j}^P + \delta T_j^B$$



$$\Delta T_j = \frac{\sum_{i=1}^{N_s} \frac{1}{\sigma_{T_i}^2} (T_{i,j} - \mu_{T_i})}{\sum_{i=1}^{N_s} \frac{1}{\sigma_{T_i}^2}}$$

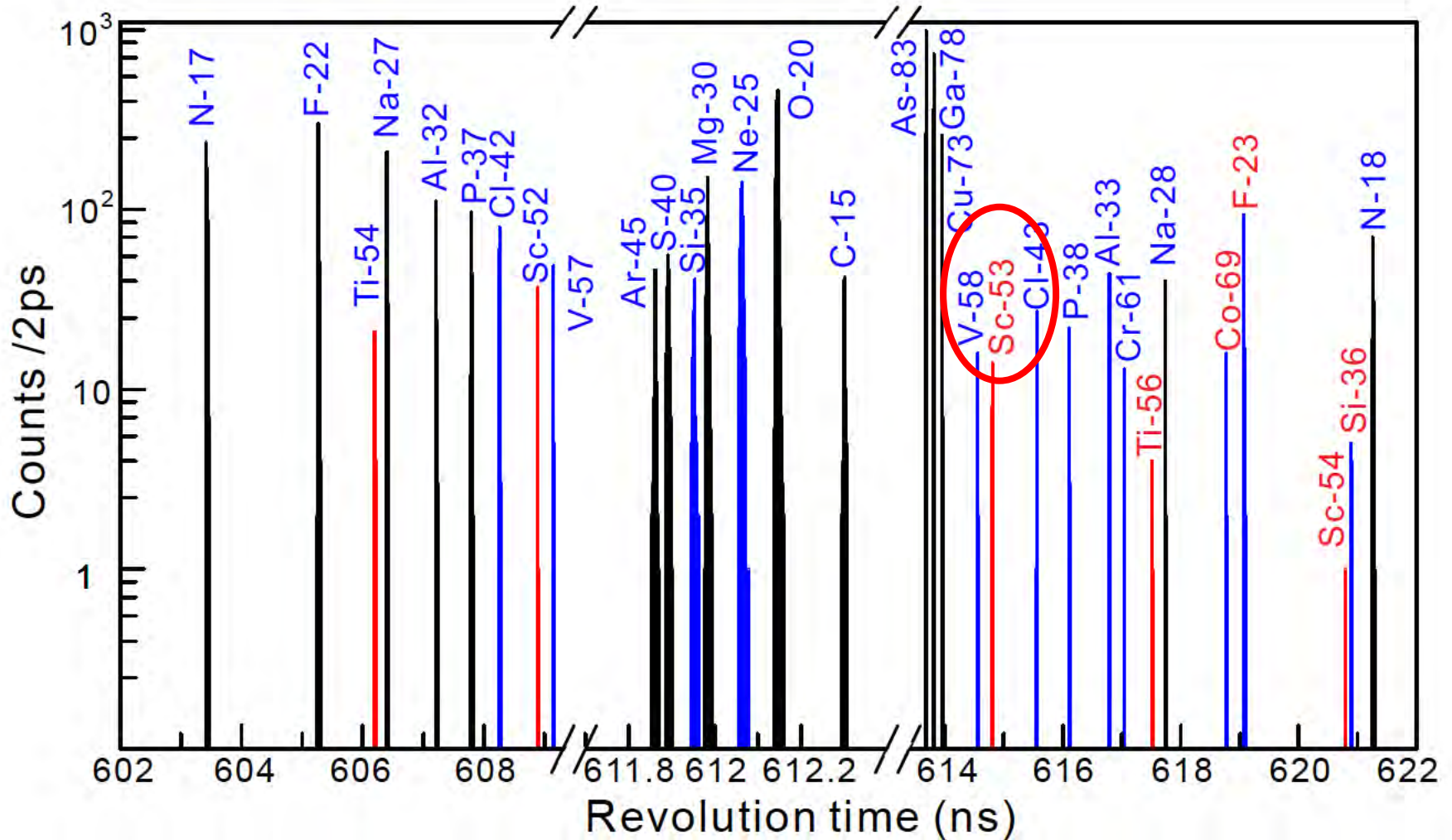
$$\sigma_{T_i}^2 = s_{T_i'}^2 + \frac{1}{\frac{1}{\sigma_{T_1}^2} + \frac{1}{\sigma_{T_2}^2} + \dots + \frac{1}{\sigma_{T_{N_s}}^2}}$$



Mass Calibration

$$m/q = a + bT + cT^2 + dT^3$$

T: Rev. Time





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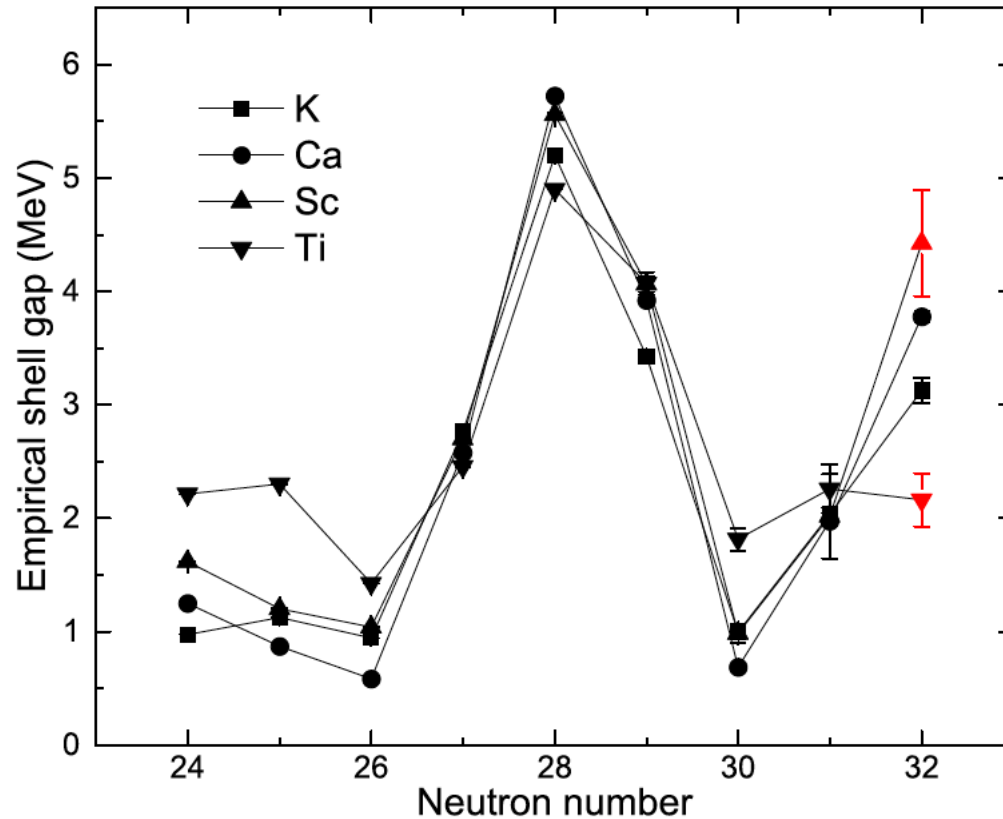
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S_{2n} and Empirical shell gap



$$S_{2n}(N, Z) = M_a(Z, N-2) + 2M_n - M_a(N, Z)$$

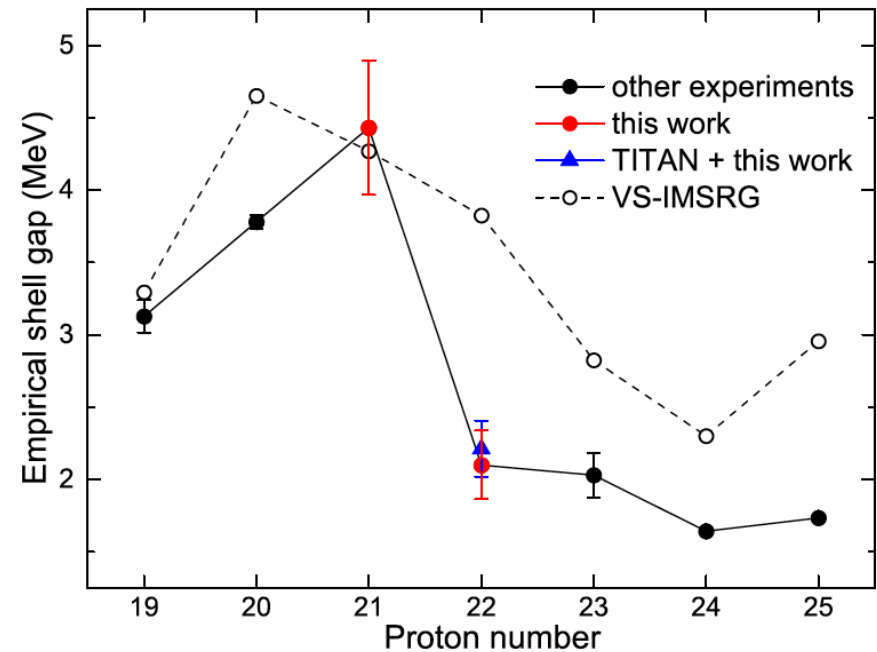
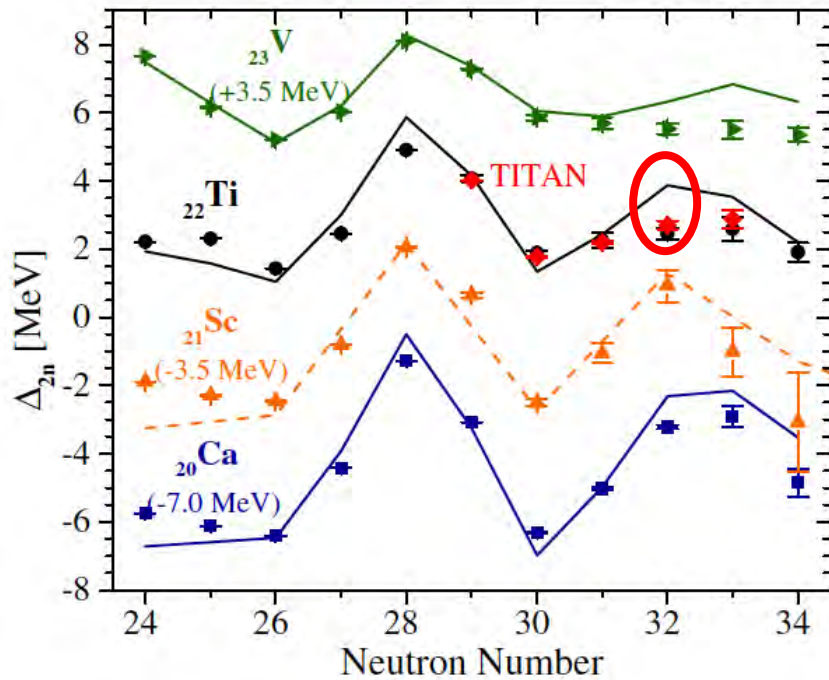
$$\Delta_{2n}(N, Z) = S_{2n}(N, Z) - S_{2n}(N+2, Z)$$

X. Xu, et al, PHYSICAL REVIEW C 99, 064303 (2019)



VS-IMSRG prediction

valence-space in-medium similarity renormalization group



E. Leistenschneider, et al, PRL 120, 062503 (2018)



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Motivation: ^{58}Ni
IMME, CDE & np interaction

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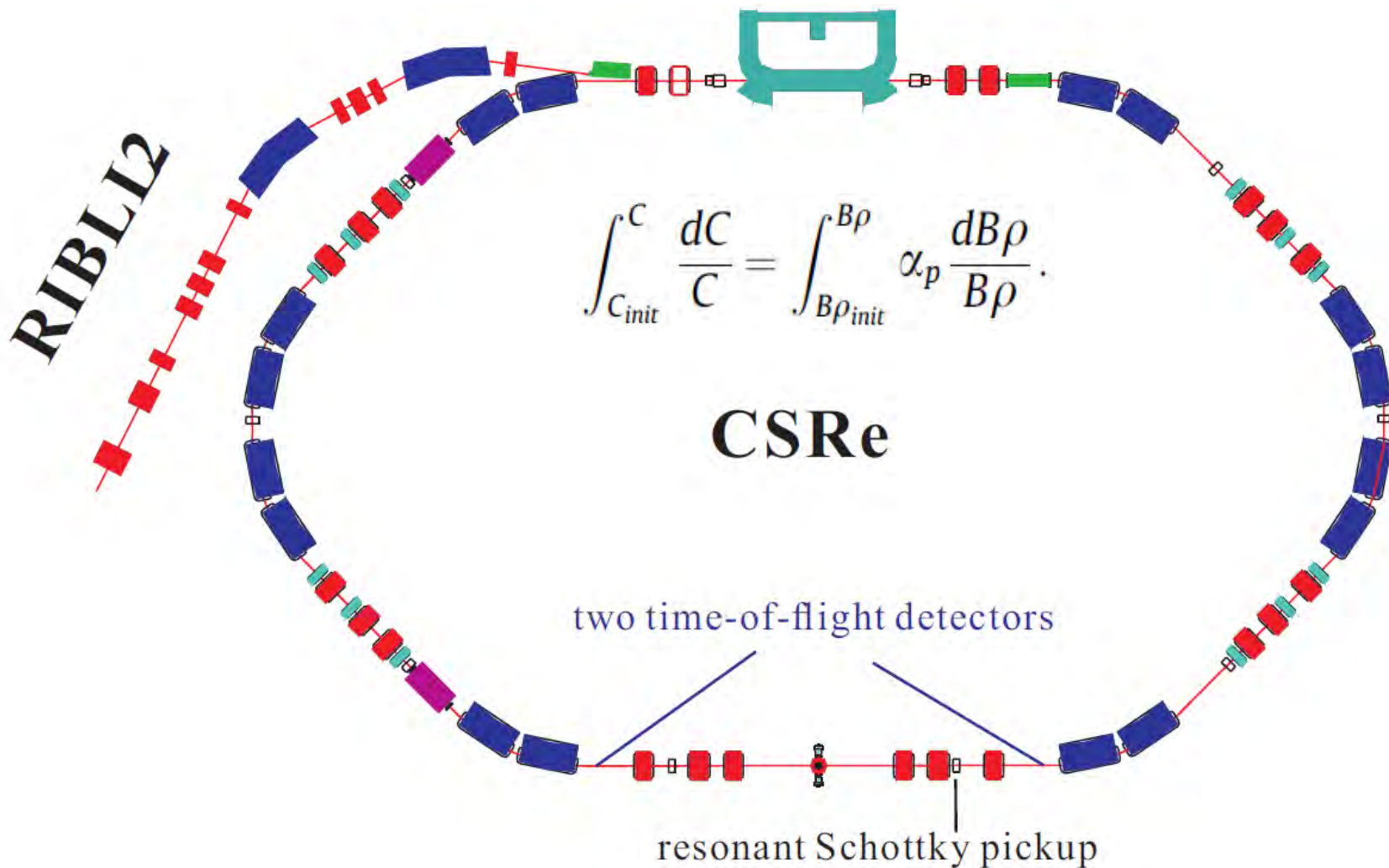
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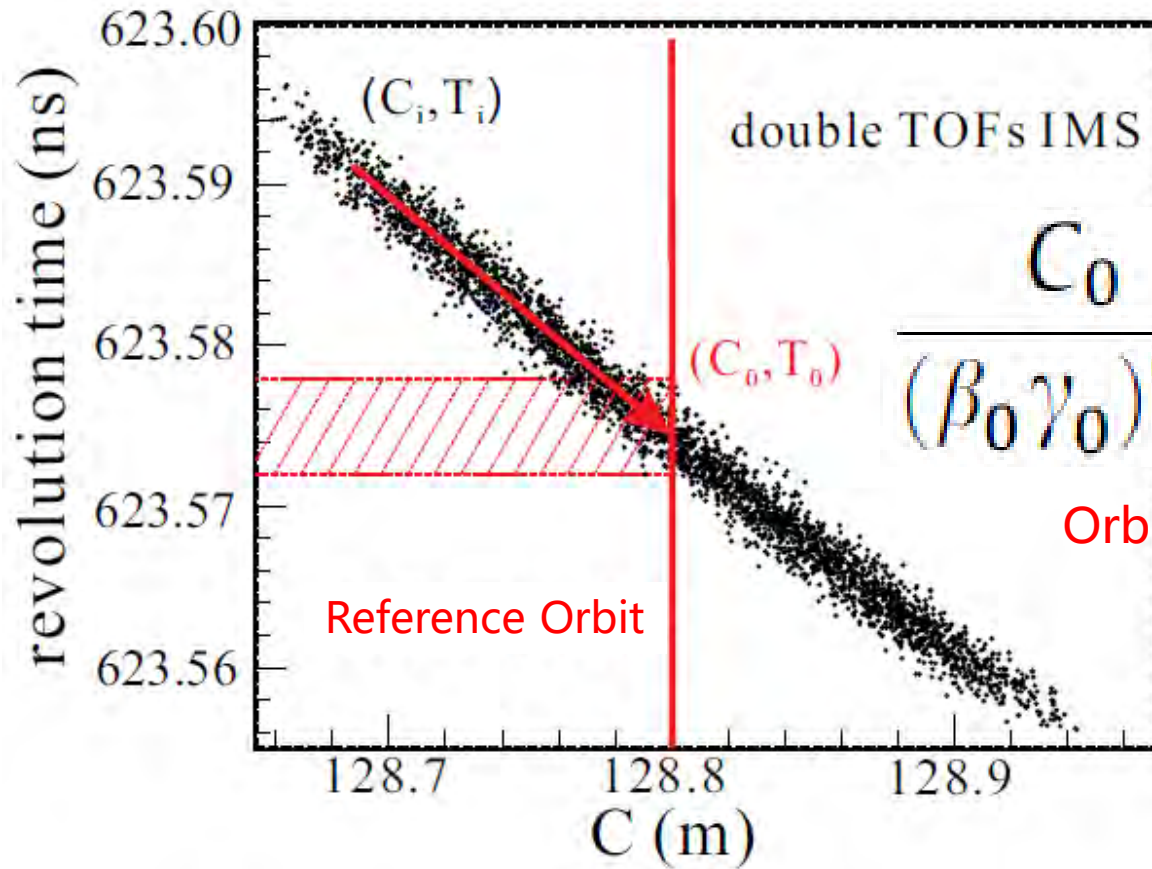
Double TOF IMS: Velocity Measurements





Double TOF IMS

Simulation data



$$\frac{C_0}{(\beta_0 \gamma_0)^{\alpha_{p0}}} = \frac{C_i}{(\beta_i \gamma_i)^{\alpha_{p0}}} = K.$$

Orbit Length

Velocity

$$C = Tv$$

Rev Time

$$\alpha_{p0} = 1/\gamma_t^2$$



Summary

- ❖ Isochronous mass spectrometry in storage ring is an ideal tool to measure the masses of short-lived nuclei:
 - no cooling required
 - single ion sensitivity
 - short half-life ~ 100 us
- ❖ Masses of ^{86}Kr PF in fp-shell have been measured in HIRFL-CSR facility in Lanzhou.
- ❖ Validate $N=32$ subshell closure in Sc isotopes.
- ❖ Shell model with tensor force between proton $f_{7/2}$ and neutron $f_{5/2}$, and ab initio calculation using the VS-IMSRG approach with NN and 3N interactions can reproduce magic number $N=32$ very well.



Collaborators

H. S. Xu, Y. H. Zhang, M. Wang, R. J. Chen, X. C. Chen, C. Y. Fu, B. S. Gao, M.Z. Sun, X. L. Tu, Y.M. Xing, X. Xu, X. L. Yan, Q. Zeng, X. H. Zhou, Y. J. Yuan, J. W. Xia, J. C. Yang, Z. G. Hu, S. Kubono, X. W. Ma, R. S. Mao, B. Mei, G. Q. Xiao, H. W. Zhao, T. C. Zhao, W. L. Zhan (IMP-CAS, Lanzhou, China)

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Y. Sun (Shanghai Jiao Tong University, Shanghai, China)

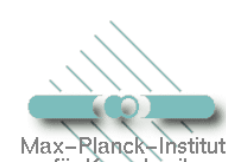
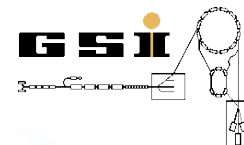
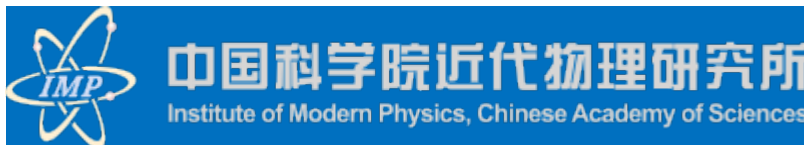
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T. Yamaguchi (Saitama University, Saitama, Japan)

T. Uesaka, Y. Yamaguchi (RIKEN, Saitama, Japan)



CSNSM

